# Computational Screening of Porous Carbons, Zeolites, and Metal Organic Frameworks for Desulfurization and Decarburization of Biogas, Natural Gas, and Flue Gas

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Eighteen kinds of porous materials from carbons, zeolites, and metal organic frameworks (MOFs) have been extensively investigated for desulfurization and decarburization of the biogas, natural gas, and flue gas by using a molecular modeling approach. By considering not only the selectivity but also capacity, Na-5A, zeolite-like MOF (zMOF), and Na-13X, MIL-47 are screened as the most promising candidates for removal of sulfide in the  $CH_4$ — $CO_2$ — $H_2S$  and  $N_2$ — $CO_2$ — $SO_2$ systems, respectively. However, for simultaneous removal of sulfide and CO<sub>2</sub>, the best candidates are zMOF for the natural gas and biogas (i.e., CH<sub>4</sub>—CO<sub>2</sub>—H<sub>2</sub>S system) and MOF-74-Zn for the flue gas (i.e., N<sub>2</sub>—CO<sub>2</sub>—SO<sub>2</sub> system). Moreover, the regeneration ability of the recommended adsorbents is further assessed by studying the effect of temperature on adsorption. It is found that compared to the zMOF and MIL-47 MOFs, the Na-5A and Na-13X zeolites are not easily regenerated due to the difficulty in desorption of sulfide at high temperature, which results from the stronger adsorbent adsorbate interactions in zeolites. The effect of sulfide concentration on the adsorption properties of the recommended adsorbents is also explored. We observe that the zMOF and MIL-47 are also superior to the Na-5A and Na-13X for desulfurization of gas mixtures containing high sulfide concentration. This is because MOFs with larger pore volume lead to a greater sulfide uptake. The effects of porosity, framework density, pore volume, and accessible surface area on the separation performance are analyzed. The optimum porosity is about 0.5–0.6, to meet the requirements of both high selectivity and uptake. It is expected this work provides a useful guidance for the practical applications of desulfurization and decarburization. © 2013 American Institute of Chemical Engineers AIChE J, 59: 2928–2942, 2013 Keywords: adsorption/gas, computer simulations (MC and MD), decarburization, desulfurization

### Introduction

In recent years, the detrimental effect of fossil fuels on human society has motivated a serious concern worldwide for the harmonious balance between energy utilization and environment protection. Generally, this issue is closely related to energy storage, carbon capture and sequestration, pollutant emission control, and novel materials for these applications. As one typical energy source, raw natural gas from wellhead contains  $CH_4$ ,  $CO_2$ ,  $N_2$ , heavier hydrocarbons,  $^{2,3}$  and hydrogen sulfide  $(H_2S)$  with a varied concentration from ppm level up to 5%. Biogas is another type of energy sources that composed of 55-70%  $CH_4$ , 30-45%

CO<sub>2</sub>, trace H<sub>2</sub>S (10-3000 ppm), and other minor components.5 Among them, CH4 is recognized to be an excellent alternative renewable clean energy. However, the existence of CO<sub>2</sub> will not only directly lead to global warming as greenhouse gas, but also reduce the energy content and particularly corrupt the transportation system in the presence of water. Consequently, CO<sub>2</sub> capture is another urgent challenge. For H<sub>2</sub>S, it is reported that exposure to this toxic gas with only 300 ppm for 30 min can cause the unconscious problem to human health.<sup>6</sup> As is well known, the H<sub>2</sub> that fuel cells require is commonly produced by catalytic reforming of natural gas to synthesis gas. If the H2S impurity in synthesis gas is not effectively reduced to a low concentration limit below 1 ppm, it will irreversibly poison the metal catalysts in both the catalytic reformers and the fuel cells electrodes. 4,7 Besides H<sub>2</sub>S contaminant, sulfur dioxide (SO<sub>2</sub>) constitutes another major contribution to air pollutant, which is mainly released from the combustion of coal and residual oil in power plants. The postcombustion gas, named flue gas

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or stack gas, typically contains several components including  $N_2,\ 10\text{--}12\%\ CO_2,\ 10\text{--}15\%\ water vapor,}\ 6\%\ O_2,\ SO_2\ (0\text{--}2000\ ppm),$  and  $NO_x\ (100\text{--}200\ ppm).^{1,8\text{--}1}$  The emissions of sulfur gas like  $H_2S$  and  $SO_2$  are responsible for the formation of acid rain and many other undesirable environmental and health hazards. Therefore, controlling their emission has become increasingly crucial importance on global atmospheric chemistry and quality of life.

A variety of processes have been developed to remove the sulfur before its emission into the atmosphere. For instance, the amine solution extraction<sup>4,7</sup> and the wet scrubbing method<sup>11</sup> using lime/limestone are the popular technologies for removing H<sub>2</sub>S and SO<sub>2</sub>, respectively. Adsorption can also be used, due to the unique advantages of less energy consumption for adsorbent regeneration, relatively simple adsorber design compared to chemical reactor, and minimum waste disposal problems.<sup>8</sup> If a suitable adsorbent is available, the adsorption approach would be competitive with other techniques mentioned above. A promising adsorbent should possess the characteristics of high sulfur selectivity and large capacity, mild operating temperature and pressure, good regenerability, high thermal stability, and tolerance to other impurities in the feed. 1,4 To date, a large number of novel porous materials have been synthesized and used for gas storage and separation, examples including porous carbons<sup>3,12–17</sup> and zeolites. <sup>6,18–27</sup>

Recently, considerable research efforts were made to metal organic frameworks (MOFs), <sup>28,29</sup> which have been regarded as the most promising microporous or/and mesoporous materials. This is because MOFs are constructed by the assembly of organic linking units with metal ions or metal clusters, and their chemical functionality and pore structures can be adjusted controllably. By tuning the length of the organic linker and varying the metal cluster, the pore volume and pore size of MOFs can be tailored over a wide atomic-scale range for special applications. These distinct advantages have substantially promoted the experimental and computational studies on the preparation and applications of MOFs. 30-37 As typical representatives, Babarao and Jiang<sup>38</sup> reported a molecular simulation study on CO<sub>2</sub> storage in ZSM-5 zeolite, single wall nanotube (SWNT), and a series of isoreticular MOFs. Similarly, Yazaydın et al.<sup>39</sup> screened 14 MOFs for CO<sub>2</sub> capture using a combined experimental and modeling approach. Hamon et al.  $^{40,41}$  investigated the adsorption of  $H_2S$  and the CH<sub>4</sub>/H<sub>2</sub>S separation in the MIL type of MOFs. Liu and Smit<sup>42</sup> performed a comparative molecular simulation study of CO<sub>2</sub>/N<sub>2</sub> and CH<sub>4</sub>/N<sub>2</sub> separation in zeolites and MOFs. Herm et al. examined the separation of CO<sub>2</sub>/H<sub>2</sub> in selected several MOFs<sup>43</sup> via adsorption experiment and ideal adsorbed solution theory (IAST) prediction.<sup>4</sup>

To the best of our knowledge, most investigations are only limited to storage of pure gases and separation of binary mixtures. However, in a practical application, the multicomponent adsorption often occurs and it is more worth studying. Unfortunately, almost no investigations were focused on the applications of desulfurization only and desulfurization/decarburization simultaneously. Moreover, the experimental measurements and the macroscopic adsorption model-based theory (e.g., IAST) are quietly difficult to study the separation of mixtures containing the trace amount (ppm) sulfur gases, because it would yield the inacceptable measuring and predicting deviations. Accordingly, here we intend to use molecular simulation method to systematically explore the neglected topic.

To achieve this target, 18 kinds of porous materials were sorted from different families of carbons, zeolites, and MOFs. The ternary mixtures of CH<sub>4</sub>—CO<sub>2</sub>—H<sub>2</sub>S and N<sub>2</sub>—CO<sub>2</sub>—SO<sub>2</sub> with a typical sulfide composition of 0.002 (2000 ppm) were adopted to mimic the real biogas, natural gas, and flue gas, respectively. This work is organized as follows. First, we describe the structures of porous materials, the potential models, and the details of molecular simulation. Second, we screen the adsorbents for the desulfurization and decarburization applications. Then, we investigate the effects of temperature and sulfur concentration on adsorption properties of recommended materials. Finally, we discuss the relation between structural properties of materials and separation selectivity.

### **Molecular Simulation**

### Sorting porous materials

The SWNT was selected here because it is one of the most important carbons<sup>12</sup> and also presents an excellent performance for capture of trace sulfur gases from binary mixtures. 46 Furthermore, our previous work indicates that another type carbon of C<sub>60</sub> intercalated graphite (CIG) behaves very well for CO2 purification, especially for N<sub>2</sub>—CO<sub>2</sub> system at room temperature, <sup>15</sup> and therefore chosen here. As typical representatives of faujasite (FAU) and Linde type families, synthetic Na-13X,<sup>23,24,47</sup> Na-5A,<sup>25,48,49</sup> and Na-4A<sup>18,20,22,26,27</sup> zeolites are considered here for their widespread use as molecular sieves and cation exchangers in catalysis and separation processes. MOF-5, <sup>29,50</sup> HKUST-1, <sup>28</sup> MIL-47(V), <sup>40,41,51,52</sup> MOF-177, <sup>53,54</sup> and COF-102<sup>55–58</sup> are selected because they are the hot topic materials and could be candidates for gas storage and separation. NOTT-103<sup>59</sup> incorporates a vacant coordination site at Cu(II) centers and has large pore volumes that contribute to high gas adsorption. ZIF-3<sup>60,61</sup> exhibits significantly higher adsorption and permeation selectivities for separation of gas mixtures compared to widely studied MOF membranes.<sup>62</sup> For ZIF-96, the nitrile and amine functional groups on the imidazolate linker lead to high CO<sub>2</sub> uptake, 63 and we conjecture that it may be a good candidate for the separation of sulfide gas. The MOF-74-M series (M=Zn, Ni, Co)<sup>64-67</sup> with the same crystal structures and different unsaturated coordinative metal centers present an ideal system to explore the roles of open metals in separation of the polar and nonpolar gas mixtures. Soc-MOF<sup>68</sup> and *rho*-zMOF<sup>69</sup> are selected because they exhibit unprecedentedly high selective adsorption for the  $\rm CO_2/CH_4$  and  $\rm CO_2/N_2$  mixtures among various MOFs and nanoporous materials.  $^{70,71}$ 

### Material structures

As mentioned previously, SWNT bundle was constructed in a diamond-like structure, <sup>46</sup> whereas CIG was built by intercalating the hexagonally aligned fullerene into three parallel graphite planes. <sup>15</sup> Zeolite 13X is composed of sodalite units interconnected through six-membered oxygen bridges (hexagonal prisms) to form a cubic lattice of supercages ~12.5 Å in diameter. <sup>24</sup> These supercages are tetrahedrally linked through 12-membered-ring windows about 7.4 Å in width. <sup>24</sup> Different number of Na<sup>+</sup> cations can be exchanged into zeolite 13X to counterbalance the negative charges due to the Al/Si substitution in the framework. In this work, 88 Na<sup>+</sup> cations per unit cell were used to represent zeolite 13X,

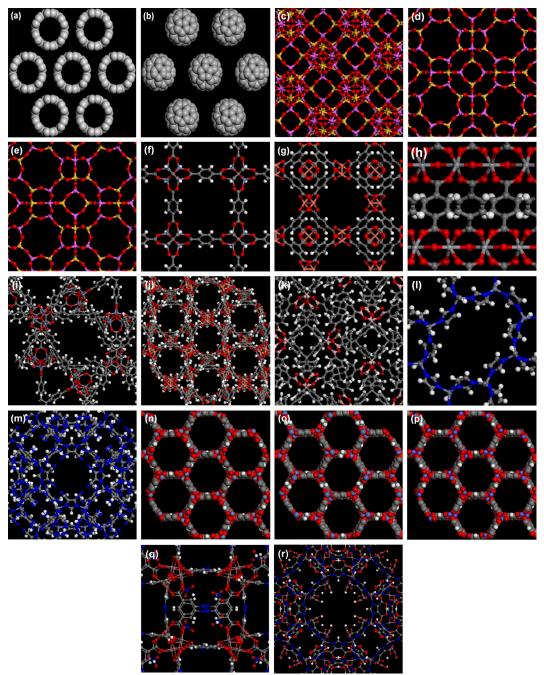


Figure 1. Material structures of (a) SWNT, (b) CIG, (c) Na-13X, (d) Na-5A, (e) Na-4A, (f) MOF-5, (g) HKUST-1, (h) MIL-47(V), (i) MOF-177, (j) NOTT-103, (k) COF-102, (l) ZIF-3, (m) ZIF-96, (n) MOF-74-Zn, (o) MOF-74-Ni, (p) MOF-74-Co, (q) soc-MOF, and (r) zMOF.

All the Na<sup>+</sup> and Ca<sup>2+</sup> ions are hidden for clarity. [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

which yields a chemical composition of  $Na_{88}Al_{88}Si_{104}O_{384}$ . The structure of Na-13X was obtained from the reported fractional coordinates of  $NaX(0)^{72}$  by randomly replacing Si by Al atoms to satisfy the Löwenstein rule, that is, all Al atoms link to 4 Si atoms via 4 O atoms and the framework Si and Al strictly alternates. Zeolites 5A and 4A are also often synthesized in the sodium form, belonging to a family of LTA-type zeolites. Their crystal unit cell consists of eight spherical  $\alpha$ -cages of  $\sim$ 11.2 Å interconnected via windows of  $\sim$ 4.1 Å in diameter. In Si/Al ratio of both zeolites is approximately equal to 1, and the composition of zeolite 4A is  $Na_{96}Al_{96}Si_{96}O_{384}$ , whereas the composition of zeolite 5A is  $Na_{32}Ca_{32}Al_{96}Si_{96}O_{384}$ , which is obtained by using 32

Ca<sup>2+</sup> and 32 Na<sup>+</sup> cations per unit cell, corresponding to a postsynthesis exchange by replacing the Na<sup>+</sup> with Ca<sup>2+</sup> cations experimentally. The crystal positions from Subramanian and Seff<sup>26</sup> and Pluth and Smith<sup>48</sup> were used for the constructions of zeolites Na-4A and Na-5A, respectively.

For MOF-5, each oxide-centered  $Zn_4O$  tetrahedron is edge-connected by six 1,4-benzenedicarboxylate linkers to form a cubic topology with cavity diameter of 14 Å.  $^{29,50}$  As to HKUST-1, copper dimers as four connectors and benzene-1,3,5-tricarboxylate as three connectors constitute  $Cu_2(COO)_4$  paddle wheels to form a three-dimensional (3-D) network with main channels of a square cross-section of 9 Å diameter and tetrahedral side pockets of 5 Å, which are

Table 1. Summary of Structural Properties for Porous Materials<sup>a</sup>

No.	Materials	Unit cell (Å)	Cell angle (°)	Number of unit cells	$(g \text{ cm}^{-3})$	$V_{\text{free}} \ (\text{cm}^3 \text{ g}^{-1})$	φ	$(m^2 g^{-1})$
1	SWNT (6,6)	a = 12.14, b = 21.027, c = 27.05	$\alpha = \beta = \gamma = 90$	$4 \times 3 \times 2$	1.53	0.25	0.38	197.7 <sup>b</sup>
2	CIG	a = 25.0, b = 21.65, c = 25.4	$\alpha = \beta = \gamma = 90$	$2 \times 3 \times 2$	1.57	0.29	0.46	343.2 <sup>b</sup>
3	Na-13X	a = b = c = 25.092	$\alpha = \beta = \gamma = 90$	$2 \times 2 \times 2$	1.42	0.39	0.55	924.1 <sup>b</sup>
4	Na-5A	a = b = c = 24.555	$\alpha = \beta = \gamma = 90$	$2 \times 2 \times 2$	1.51	0.35	0.53	721.0 <sup>b</sup>
5	Na-4A	a = b = c = 24.584	$\alpha = \beta = \gamma = 90$	$2 \times 2 \times 2$	1.52	0.33	0.51	710.6 <sup>b</sup>
6	MOF-5	a = b = c = 25.832	$\alpha = \beta = \gamma = 90$	$2 \times 2 \times 2$	0.59	1.35	0.80	3365.1°
7	HKUST-1	a = b = c = 26.343	$\alpha = \beta = \gamma = 90$	$2 \times 2 \times 2$	0.88	0.80	0.71	$2134.0^{c}$
8	MIL-47(V)	a = 6.818, b = 16.143, c = 13.939	$\alpha = \beta = \gamma = 90$	$6 \times 3 \times 4$	1.0	0.61	0.61	1511.7 <sup>c</sup>
9	MOF-177	a = b = 37.072, c = 30.033	$\alpha = \beta = 90, \gamma = 120$	$1 \times 1 \times 1$	0.43	1.93	0.82	$4833.0^{\circ}$
10	NOTT-103	a = b = 18.513, c = 45.354	$\alpha = \beta = 90, \gamma = 120$	$2 \times 2 \times 1$	0.64	1.15	0.74	3646.4 <sup>b</sup>
11	COF-102	a = b = c = 27.177	$\alpha = \beta = \gamma = 90$	$2 \times 2 \times 2$	0.42	1.83	0.77	5129.5 <sup>b</sup>
12	ZIF-3	a = b = 18.97, c = 16.74	$\alpha = \beta = \gamma = 90$	$2 \times 2 \times 2$	0.88	0.75	0.66	1902.3 <sup>b</sup>
13	ZIF-96	a = b = c = 28.3564	$\alpha = \beta = \gamma = 90$	$1 \times 1 \times 1$	0.98	0.60	0.59	1197.1 <sup>b</sup>
14	MOF-74-Zn	a = b = 25.932, c = 6.837	$\alpha = \beta = 90, \gamma = 120$	$2 \times 2 \times 4$	1.22	0.54	0.65	1324.4°
15	MOF-74-Ni	a = b = 25.786, c = 6.77	$\alpha = \beta = 90, \gamma = 120$	$2 \times 2 \times 4$	1.19	0.54	0.64	1456.3°
16	MOF-74-Co	a = b = 26.11, c = 6.719	$\alpha = \beta = 90, \gamma = 120$	$2 \times 2 \times 4$	1.18	0.55	0.65	1508.2°
17	soc-MOF	a = b = c = 22.457	$\alpha = \beta = \gamma = 90$	$2 \times 2 \times 2$	1.12	0.57	0.64	1441.2 <sup>b</sup>
18	zMOF	a = b = c = 31.062	$\alpha = \beta = \gamma = 90$	$1 \times 1 \times 1$	1.19	0.51	0.61	1069.1 <sup>b</sup>

 $^{a}\rho_{\rm f}$  is the framework density,  $V_{\rm free}$  is the free pore volume, and  $\phi$  is the porosity expressed by the ratio of the free volume of adsorbent accessible to gas molecules to the adsorbent volume. In the present work, the free volume is calculated by a Monte Carlo integration with the reentrant surface definition,  $^{15,74}$  where the argon molecule with a size of 3.4 Å was used as a probe.  $S_a$  is the accessible surface area calculated by the method of Düren et al., where the nitrogen probe with a diameter of 3.681 Å was used.

This work.

linked to the main channels by triangular windows of 3.5 Å diameter.<sup>28</sup> Isostructural MIL-47(V) is built up from cornersharing  $V^{4+}O_6$  octahedra interconnected by terephthalate groups, forming a 3-D framework with a one-dimensional (1-D) diamond-shaped channels of diameter  $\sim 8.5$  Å.<sup>51</sup> MOF-177 material consists of tetrahedral [Zn<sub>4</sub>O]<sup>6+</sup> clusters linked by the tritopic linker 1,3,5-benzenetribenzoate, with a very high surface area about 4500 m<sup>2</sup> g<sup>-1</sup>.<sup>53</sup> NOTT-103 is an isostructural polymers of composition  $C_{35}H_{43}Cu_2N_3O_{16}$ , which contains binuclear Cu(II) paddlewheel nodes each bridged by four carboxylate centers to yield a NbO-type network.<sup>59</sup> COF-102 has a cubic structure constructed completely from strong covalent bonds by joining of the triangular and tetrahedral nodes, with a crystal density 0.41 g cm<sup>-3</sup> and a largest cavity of 5.66 Å. 56,73 ZIF-3 framework, consisted of zinc and imidazolate linkers, has a zeolite DFT topology,60 whereas ZIF-96, built from the functionalized imidazoles C<sub>4</sub>H<sub>4</sub>N<sub>4</sub> cyamIm linker, is based on the zeolite RHO topology.<sup>63</sup> MOF-74-M (M=Zn, Ni, Co) is composed of M<sup>+2</sup> cation bridged by the carboxylate and oxy- groups of fully deprotonated 2,5-dihydroxybenzene-1,4-dicarboxylic acid, having linked chains that are arranged in a parallel and hexagonal 1-D pore (diameter ~12 Å). 64-67 The metal centers are bonded to five oxygen atoms in a square-pyramid coordination. socMOF is synthesized by an indium trimer building block, resulted in a narrow pore diameter of about 12 Å, a composition of  $[In_3O(C_{16}N_2O_8H_6)_{1.5}]$ -(NO<sub>3</sub>), and a soc topology characterized by its square-octahedral connectivity net. 68 The ionically bound nitrate anions proximal to the indium trimer give the framework a highly ionic character. rho-zMOF, a representative of zeolite-like MOFs (zMOFs) with a topology of *rho*-zeolite used in this work, is synthesized by metal-ligand-directed assembly of In atoms and 4,5-imidazoledicarboxylic acid (H3ImDC).<sup>69</sup> It is obtained by substituting oxygen atoms in zeolites by organic linkers, so the structure is similar to inorganic zeolites but

with an extra-large cavities size of 18.2 Å. zMOFs contain the charged frameworks and charge-balancing extra framework ions that can increase the interactions with guest molecules and consequently enhance the storage and separation capability of this material. A canonical ensemble MC simulation at 303 K was performed to characterize the locations of Na<sup>+</sup> ions in zMOF. Initially, 48 Na<sup>+</sup> ions were inserted randomly into the system followed by 10<sup>7</sup> trial displacement moves. The acceptance criteria for the trial moves were based on the Metropolis algorithm. All the structures of the selected MOFs were constructed from their corresponding experimental XRD data, and the CIF format files can be downloaded from the Cambridge Crystallographic Data Centre. The atomic structures of all the adsorbents are shown in Figure 1, and their lattice constants, crystal densities, pore volumes, and porosities are summarized in Table 1.

### Force fields

The fluid-fluid interactions of the species are composed of the Lennard-Jones (LJ) and electrostatic interactions. In the present work, we used the same potential models for fluids as our previous work, 46 that is, the spherical united-atom LJ model to represent N2 and CH4, and three-site rigid model to represent CO2, H2S, and SO2. Generally speaking, the united-atom LJ model (namely, one-site model) can save much computational time compared to the all-atom model, and thus is preferentially chosen if the computational accuracy can be maintained. Our recent study<sup>76</sup> on adsorption properties of the UMCM-1 material indicates that the simulated CH<sub>4</sub> isotherms with the one-site model can reproduce well the corresponding experimental data, and in particular, the one-site model is more accurate than the three-site model for N2. Here, we used the one-site potential parameters from Babarao et al. <sup>77</sup> for CH<sub>4</sub> and Peng et al. <sup>13</sup> and Kaneko and coworkers <sup>78</sup> for N<sub>2</sub>. In the three-site rigid models for CO<sub>2</sub>, H<sub>2</sub>S, and SO<sub>2</sub>, a three-site LJ potential plus a set of partial

<sup>&</sup>lt;sup>c</sup>From the work of Yazaydin et al.<sup>39</sup>

point charges are distributed at three electrostatic sites. The linear CO<sub>2</sub> molecule was described by the elementary physical model,<sup>79,80</sup> where the C—O bond length is 1.149 Å, the partial point charge on the C atom is +0.6512e, and electric neutrality is maintained the partial charge of -0.3256e on O atom. The H<sub>2</sub>S molecule was represented by the three-site model from Nath's work,<sup>81</sup> in which the H—S bond length and H—S—H bond angle are 1.365 Å and 91.5°, with the point charges of +0.124e and -0.248e on H and S sites. Similarly, in Ribeiro's potential model<sup>82</sup> for SO<sub>2</sub> molecule, the S—O bond length and the O—S—O bond angle are 1.4321 Å and 119.5°, and the partial charges on S and O atoms are +0.470e and -0.235e.

For porous carbons, the size and energy parameters of 3.4 Å and 28.0 K were used for the carbon atom in SWNT and CIG adsorbents. In all the three zeolites, only electrostatic potential was taken into account for the interactions between the adsorbates and the framework Si and Al atoms. 22,24,49 In addition, for the O atom in zeolites, the LJ parameters of 2.806 Å and 89.6 K from Goj et al.<sup>22</sup> were used, whereas for Na<sup>+</sup> ions, 2.85 Å and 8.0 K were taken from Akten et al. 18 In Na-5A zeolite, the LJ parameters and point charge were given as 3.037 Å, 50.0 K, and +2e for  $Ca^2 + ions$  according to Ohba et al. 83 The partial charges associated with other framework atoms refer to the work of Granato et al.,<sup>24</sup> García-Pérez et al.,<sup>49</sup> and Akten et al.<sup>18</sup> for Na-13X, Na-5A, and Na-4A, respectively. The dispersive interactions of all the atoms in MOFs are described by directly applying the universal force field (UFF) from Rappe et al.,84 rather than using the one that has been validated in the literatures or refining the potential parameters ourselves. This is based on the following three considerations. First, in the case of without refinement, UFF also yields a good representation of the measured adsorption isotherms for the MOFs. 76,77 Second, the refinement strategy should be executed for every adsorbate-adsorbent interaction to meet the consistency principle of force field development, not limited to the systems with available experimental data only. Unfortunately, almost no experimental adsorption data of H2S and SO2 in MOFs is available. Third, the experimental isotherms reported by different research groups may also vary for the same gas due to the differences of the MOFs sample preparation and activation.<sup>39</sup> The Na<sup>+</sup> ions in zMOF have the LJ parameters and partial point charge of 2.658 Å, 15.09 K, and +1e, which are the same as Babarao and Jiang. <sup>71</sup> For MOF-5, HKUST-1, MIL-47(V), MOF-177, and MOF-74 series, the charge data from Yazaydın et al.<sup>39</sup> were used here, whereas for COF-102, soc-MOF, and zMOF adsorbents, they are taken from Babarao et al. 70 and Babarao and Jiang's 71,73 works. For ZIF series, we adopted the charge from Keskin<sup>62</sup> and Morris et al.<sup>63</sup> for ZIF-3 and ZIF-96, respectively. For NOTT-103 material, ab inito calculations were performed using the Gaussian 03 software<sup>85</sup> to calculate the point charges of the atoms in the framework (see Figure S0 in Supporting Information for details). All the force field parameters were summarized in Table 2 and the Lorentz-Berthelot combining rules were used to calculate the cross LJ interactions.

### Simulation details

Grand canonical Monte Carlo (GCMC) simulations<sup>86,87</sup> were performed to investigate the adsorption and separation of gases in porous materials. During the simulations, the

Table 2. Force Field Parameters for Adsorbates and Adsorbents

			u h		. 1	91.1
			ε/k <sup>b</sup>		Angle	<sup>a</sup> bl
Adsorbate	Atom	σ (Å)	(K)	q (e)	(°)	(Å)
$N_2$		3.549	94.95			
$CH_4$		3.73	148.0			
$CO_2$	C	2.789	29.66	+0.576	180	1.18
	O	3.011	82.96	-0.288		
$H_2S$	Н	0. 98	3.9	+0.124	91.5	1.365
	S	3.72	250.0	-0.248		
$SO_2$	S	3.585	154.4	+0.470	119.5	1.4321
	O	2.993	62.3	-0.235		
Carbons	C	3.4	28.0			
Zeolites	O	2.806	89.6	a		
	Na	2.85	8.0	a		
	Ca	3.037	50.0	a		
MOFs	C	3.431	52.791	a		
	Н	2.571	22.122	a		
	O	3.118	30.166	a		
	N	3.261	34.722	a		
	В	3.638	90.498	a		
	V	2.801	8.051	a		
	Zn	2.462	62.343	a		
	Cu	3.114	2.516	a		
	Co	2.559	7.045	a		
	Ni	2.525	7.548	a		
	Na	2.658	15.09	a		
	In	3.976	301.429	a		

<sup>a</sup>bl is the bond length. The partial charges for atoms on porous material are given in the text.

adsorbents were treated as a rigid material with atoms frozen. The periodic boundary conditions were imposed in three dimensions to mimic the crystal periodicity. The spherical cutoffs of 12.0 Å for carbon/zeolites and 12.8 Å for MOFs were used to calculate the intermolecular LJ interactions without long-range corrections. 42 For orthogonal systems, the electrostatic interaction between adsorbate and adsorbent was handled by using the Ewald summation technique, whereas for non-orthogonal systems and the electrostatic interaction between adsorbates, Wolf spherically truncated method<sup>88</sup> was used and the cutoff was set as the same as that of the LJ interactions. To accelerate the simulation, the LJ and electrostatic interactions between adsorbate and adsorbent were interpolated from a pretabulated energy map with a grid spacing 0.2 Å. A total of  $2 \times 10^7$ configurations were generated for each pressure point. The first  $1 \times 10^7$  configurations were discarded to guarantee equilibration and the second one was divided into 20 blocks to calculate the ensemble average. For N2 and CH4 with sphere geometry, only three types of moves including translation, insertion, and deletion are attempted, whereas for other molecules with three-site potential models, an additional rotation move is implemented. All the GCMC simulations were conducted by using the MUSIC code.<sup>89</sup> The normal move acceptance probability is transformed to relate the component fugacity of bulk phase by Peng-Robinson equation of state (PR EOS). 90 Therefore, the fugacity rather than chemical potential is used as an input parameter in the simulations. The critical properties and the binary interaction parameters of PR EOS are given in Supporting Information Table S1.

All the uptakes are reported as the absolute adsorption amount. To investigate the separation ability of porous material for gas mixtures, we defined three adsorption selectivities as follows

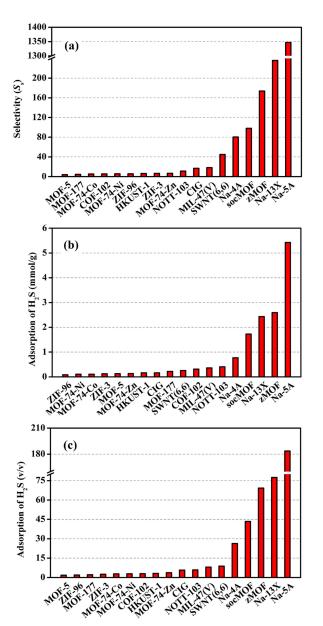


Figure 2. Removal of sulfide from the  $CH_4$ — $CO_2$ — $H_2S$  system ( $y_{CH_4} = 0.7$  and  $y_{H_2S} = 0.002$ ) in the recommended porous materials at 4 MPa and 303 K.

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$$S_{i/j} = \frac{x_i/x_j}{y_i/y_j} \tag{1}$$

$$S_{s} = \frac{x_{s}(1 - y_{s})}{y_{s}(1 - x_{s})} \tag{2}$$

$$S_{sc} = \frac{(x_s + x_{co_2})(1 - y_s - y_{co_2})}{(y_s + y_{co_2})(1 - x_s - x_{co_2})}$$
(3)

where  $S_{i/j}$  refers to the selectivity of the first component i over the second component j,  $S_{\rm s}$  denotes the desulfurization ability stand alone,  $S_{\rm sc}$  denotes the desulfurization and decarburization ability simultaneously, the subscript S means the sulfide gas of  $\rm H_2S$  or  $\rm SO_2$ , and the x, y denote the molar fractions of species in the adsorbed and bulk phases, respectively.

### **Results and Discussions**

### Pairwise adsorption selectivities and the component isotherms

As mentioned before, we first consider the removal of trace sulfur of biogas, which mainly contains CH<sub>4</sub>, CO<sub>2</sub>, and H<sub>2</sub>S, and postcombustion flue gas which mainly contains N<sub>2</sub>, CO<sub>2</sub>, and SO<sub>2</sub>, and therefore, investigate the two corresponding ternary mixture systems and the pairwise adsorption selectivity in the two ternary mixture systems. Supporting Information Figures S1–S18 show the pairwise adsorption selectivities and the component isotherms of CH<sub>4</sub>—CO<sub>2</sub>—H<sub>2</sub>S and N<sub>2</sub>—CO<sub>2</sub>—SO<sub>2</sub> systems in 18 materials of MOF-5, HKUST-1, MIL-47(V), ZIF-3, ZIF-96, COF-102, MOF-177, NOTT-103, SWNT(6,6), CIG, Na-13X, Na-5A,

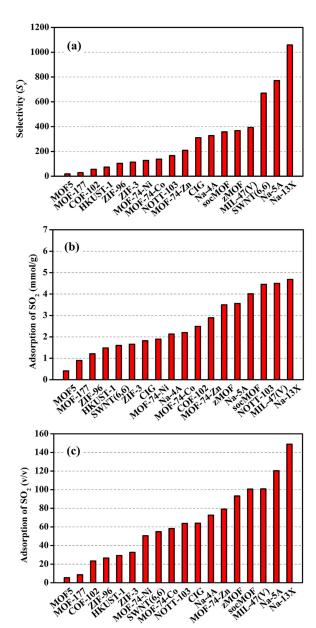


Figure 3. Removal of sulfide from the  $N_2$ — $CO_2$ — $SO_2$  system ( $y_{N_2} = 0.8$  and  $y_{SO_2} = 0.002$ ) in the recommended porous materials at 4 MPa and 303 K.

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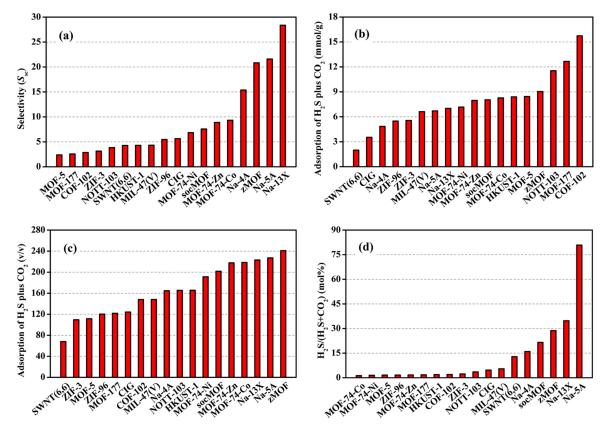


Figure 4. Simultaneous removal of sulfide and  $CO_2$  from the  $CH_4$ — $CO_2$ — $H_2S$  system ( $y_{CH_4} = 0.7$  and  $y_{H_2S} = 0.002$ ) in the recommended porous materials at 4 MPa and 303 K.

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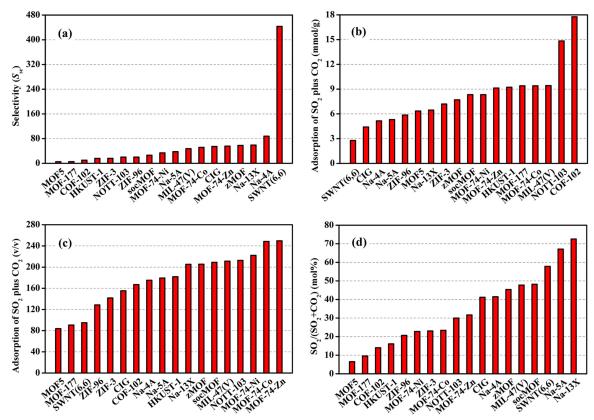


Figure 5. Simultaneous removal of sulfide and  $CO_2$  from the  $N_2$ — $CO_2$ — $SO_2$  system ( $y_{N_2}$  = 0.8 and  $y_{SO_2}$  = 0.002) in the recommended porous materials at 4 MPa and 303 K.

[Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

Table 3. Recommended Porous Materials for Removal of Sulfide only and Simultaneous Removal of Sulfide and CO<sub>2</sub>

System	Removal of sulfide	Simultaneous removal of sulfide and CO <sub>2</sub>		
Biogas and nature gas (CH <sub>4</sub> —CO <sub>2</sub> —H <sub>2</sub> S)	Na-5A, zMOF	zMOF		
Flue gas $(N_2 - CO_2 - SO_2)$	Na-13X, MIL-47	MOF-74-Zn		

Na-4A, MOF-74-Zn, MOF-74-Co, MOF-74-Ni, socMOF, and zMOF at 303 K, respectively, where the bulk gas molar ratio of the  $CH_4$ – $CO_2$ – $H_2S$  system is 0.7:0.298:0.002;  $N_2$ - $CO_2$ - $SO_2$ that of the system is 0.8:0.198:0.002. Apparently, the selectivity of H<sub>2</sub>S/CH<sub>4</sub> in the CH<sub>4</sub>-CO<sub>2</sub>-H<sub>2</sub>S system and the one of SO<sub>2</sub>/N<sub>2</sub> in the N<sub>2</sub>-CO<sub>2</sub>-SO<sub>2</sub> system are always the largest, because H<sub>2</sub>S and SO<sub>2</sub> are the most preferentially adsorbed, whereas CH<sub>4</sub> and N2 are the most unfavorably adsorbed in their corresponding ternary mixtures. Accordingly, these selectivities span several orders of magnitude from 10 to 10<sup>6</sup> for different pairwises. Furthermore, the shapes of the selectivity curves exhibit apparently different behavior such as monotonically ascending or descending with the increase of pressure, which is strongly dependent on the types of the materials. However, at high pressure the selectivities gradually reach a stable plateau. Among the species of ternary mixtures, CO2 almost occupies the largest adsorption capacity for all the adsorbents, except that the uptakes of sulfide gases are the greatest in SWNT and Na-13X for  $N_2$ — $CO_2$ — $SO_2$  and in Na-5A for both systems. In the latter, the sulfide uptake quickly reaches saturation at low pressure near zero, indicating that the adsorption isotherms can be classified as type I for micropore filling. These observations above give us a chance to screen the more suitable candidate for desulfurization and decarburization of biogas and postcombustion flue gas.

### Screening adsorbents for removal of sulfide only

To evaluate the separation ability of various adsorbents, the adsorption data at 4 MPa are chosen to obtain the optimization for both the uptake and the selectivity, because the pressure is acceptable for industrial applications. Figures 2 and 3 show the desulfurization selectivity alone of  $S_s$ , and the sulfide uptakes in both gravimetric and volumetric units for CH<sub>4</sub>-CO<sub>2</sub>-H<sub>2</sub>S and N<sub>2</sub>-CO<sub>2</sub>-SO<sub>2</sub> systems, respectively. For H<sub>2</sub>S removal, zMOF, socMOF and all the three zeolites dominate the top five for both selectivity and uptake (see Figure 2), which is because all the five adsorbents have intrinsic ionic characteristics which can enhance the material affinity towards guest molecules. Among them, Na-5A ranks the first and especially its  $S_s$  is 4.7 times more than the second one of Na-13X, reaching up to an extraordinary high value of 1347. The big difference between both adsorbents is mainly derived from the fact that Na-5X contains two types of Na<sup>+</sup> and Ca<sup>2+</sup> ions which can simultaneously contribute to the adsorption of H<sub>2</sub>S. Nevertheless, only Na<sup>+</sup> ions are included in Na-13X and thus the greater desulfurization

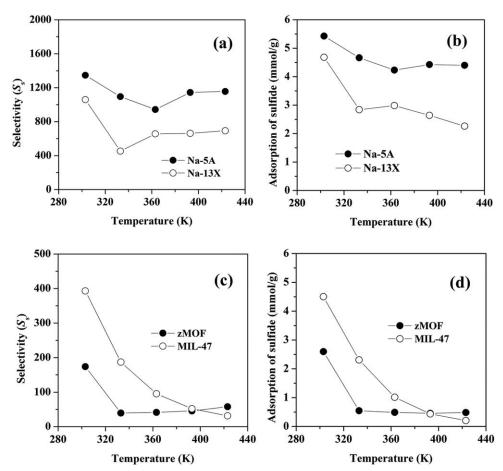


Figure 6. Effect of temperature on removal of sulfide in the recommended porous materials at 4 MPa, where the closed and open symbols denote the CH<sub>4</sub>—CO<sub>2</sub>—H<sub>2</sub>S and N<sub>2</sub>—CO<sub>2</sub>—SO<sub>2</sub> systems, respectively.

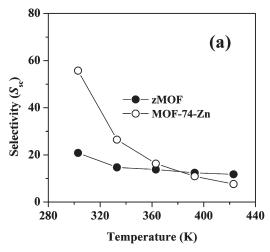
selectivity is anticipated to be Na-5X, despite that both of them belong to the same family of zeolite.

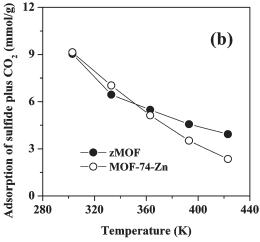
Besides the ionic characteristic of adsorbents, another factor that affects the sulfide purification is the confinement effect (i.e., pore size and volume of a porous material) and functionalization of the surface. This is typically reflected in SWNT and CIG materials. Since there is no modification of polar functional groups on the smooth surface of these carbons, these carbons are not the best for the desulfurization. However, we can see from Figure 2 that their selectivities and uptakes are even better than several MOFs like HKUST-1 and ZIF-96, which possess the exposed metal centers or polar functional groups to favor the adsorption separation. This can be explained by the fact that both SWNT and CIG have very small micorpore, which is less than half of HKUST-1 and ZIF-96 in pore volume (see Table 1). That is to say, in this case, the confinement effect of the two carbon materials is stronger, and accordingly it plays an important role in determining the separation ability.

As shown in Figure 2, among the top five adsorbents, zMOF is superior to socMOF and Na-4A in both selectivity and uptake. Although its selectivity is about 26% lower than that of Na-13X, its volumetric uptake is comparable to Na-13X, and zMOF even exceeds Na-13X in the gravimetric uptake. Therefore, Na-5A from zeolites family and zMOF from MOFs family are recommended for H2S removal. For  $SO_2$  removal, the top five selectivity  $S_s$  is Na-13X > Na-5A > SWNT > MIL-47(V) > zMOF (see Figure 3a). Different from H<sub>2</sub>S removal, here Na-13X exhibits the greatest selectivity rather than Na-5A. The reason is that SO2 has a bigger molecule size than H<sub>2</sub>S (see Table 2), and therefore Na-13X with a slightly larger pore volume (see Table 1) can accommodate more number of SO2 molecules. The uptake data in Figure 3b and c also convince this point of view. The selectivity of SWNT is only less than that of Na-13X and Na-5A. However, its gravimetric uptake falls into the bottom and thus it is excluded from the recommended list. The selectivity of MIL-47(V) is only a half of Na-5A, but it has a considerably high selectivity of 393, which is better than zMOF for desulfurization. More importantly, MIL-47(V) has the second greatest gravimetric uptake after Na-13X and is about 21% higher than that of Na-5A. As a consequence, to remove the  $SO_2$  impurity in  $N_2$ – $CO_2$ – $SO_2$ system, we recommend Na-13X and MIL-47(V) materials from zeolites and MOFs families.

# Screening adsorbents for removal of sulfide and CO<sub>2</sub> simultaneously

Figures 4 and 5 present the sulfide,  $CO_2$  uptakes and the selectivities  $S_{sc}$  of desulfurization and decarburization simultaneously in  $CH_4$ — $CO_2$ — $H_2S$  and  $N_2$ — $CO_2$ — $SO_2$  systems, respectively. We can see from Figure 4a that the descending order of the top five  $S_{sc}$  is Na-13X, Na-5A, zMOF, Na-4A, and MOF-74-Co. By contrast, the descending order of sulfide and  $CO_2$  uptake is COF-102, MOF-177, NOTT-103, zMOF, and MOF-5 (see Figure 4b). For the latter (i.e. the second list), all the zeolites are excluded because their gravimetric uptakes are lower than a half of these MOF and COF materials. Similarly, COF-102, MOF-177, NOTT-103, and MOF-5 are eliminated from the first list for their worse selectivities  $S_{sc}$ . Although the gravimetric uptake of MOF-74-Co is slightly smaller than zMOF, the selectivity of zMOF is almost twice of the former, and therefore MOF-74-Co is also





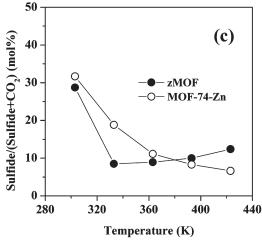


Figure 7. Effect of temperature on removal of sulfide and CO<sub>2</sub> in the recommended porous materials at 4 MPa, where the closed and open symbols denote the CH<sub>4</sub>—CO<sub>2</sub>—H<sub>2</sub>S and N<sub>2</sub>—CO<sub>2</sub>—SO<sub>2</sub> systems, respectively.

not recommended. Clearly, in the two lists, only zMOF adsorbent can satisfy the requirements of both selectivity and uptake. It should be noted that zMOF also owns the best volumetric uptake of 240 v/v (see Figure 4c), which is exactly consistent with the above conclusions. Figure 4d shows the mole percentages of  $\rm H_2S$  in the  $\rm H_2S$  and  $\rm CO_2$  total uptake. It is found that  $\rm H_2S$  adsorption is absolutely dominant in

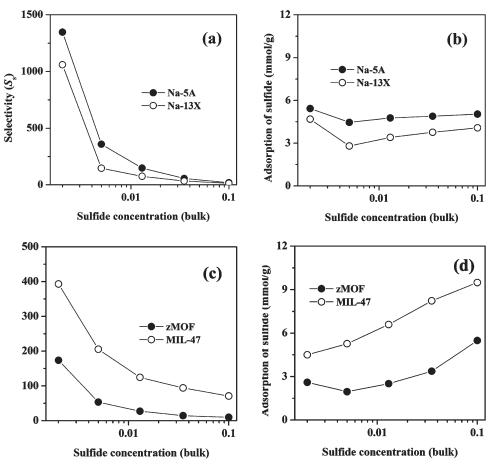
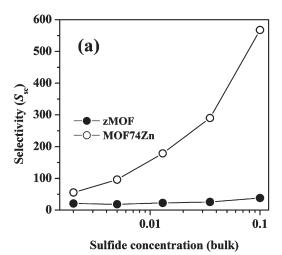


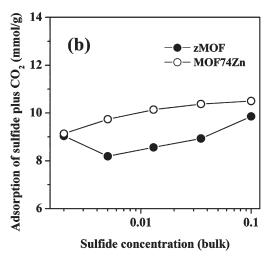
Figure 8. Effect of sulfide mole fraction in bulk phase on removal of sulfide in the recommended porous materials at 4 MPa, where the closed and open symbols denote the CH<sub>4</sub>—CO<sub>2</sub>—H<sub>2</sub>S and N<sub>2</sub>—CO<sub>2</sub>—SO<sub>2</sub> systems, respectively.

Na-5A and occupies 80.9% of the total uptake. On the contrary, except  $H_2S$ ,  $CO_2$  is the major constituent in the zMOF pore, reaching 71.3% of the total uptake. Considering the trace  $H_2S$  concentration in the bulk phase, it seems that zMOF shows a good purifying ability for both  $H_2S$  and  $CO_2$  gases. For most adsorbents of from MIL-47(V) to MOF-74-Co, the  $H_2S$  amounts are less than 5.4%, indicating that these materials give priority to decarburization other than desulfurization.

As shown in Figure 5a, for the  $N_2$ — $CO_2$ — $SO_2$  system, the descending order of the top five S<sub>sc</sub> is SWNT, Na-4A, Na-13X, zMOF, and MOF-74-Zn. In particular, due to the strong confinement effect, SWNT exhibits an extremely high selectivity of 443, about five times of the second one of Na-4A. In the view of gravimetric uptake, COF-102 is the best and the following is NOTT-103. Moreover, the materials from MIL-47(V) to MOF-74-Zn belong to the same level, because their uptakes approximate to each other and are around 9 mmol g<sup>-1</sup>. Applying the similar screening strategy mentioned above, we only keep MOF-74-Zn, MOF-74-Co, and MIL-47(V) in the two lists. A further observation on Figure 5a and c shows that among the three adsorbents, MIL-47(V) is the worst at the selectivity and volumetric uptake, and it thus is not recommended. Meanwhile, MOF-74-Zn has a better selectivity and volumetric uptake and a slightly lower gravimetric uptake, compared to MOF-74-Co. Consequently, we propose that MOF-74-Zn is a more promising adsorbent for simultaneous removal of  $SO_2$  and  $CO_2$ . Figure 5d shows the percentages of  $SO_2$  in the  $SO_2$  and  $CO_2$  total uptake. Interestingly, we found some similar behavior as in the  $CH_4$ — $CO_2$ — $H_2S$  system. First, the adsorbent with the greatest sulfide percentage, in which the sulfide is absolutely preferentially adsorbed, may be not appropriate for decarburization and desulfurization. For example, here Na-13X has a 72.6%  $SO_2$  content in the total uptake. Second, a suitable adsorbent for simultaneous removal of sulfide and  $CO_2$  usually can reach a compromise between the competitive adsorptions of both species. In other words, it not only adsorbs a major of  $CO_2$  molecules, but also contains a certain capacity of sulfide. In this case,  $CO_2$  content in MOF-74-Zn reaches 69% and the  $SO_2$  content is about 31%. It also coincides with that of zMOF in the  $CH_4$ — $CO_2$ — $H_2S$  system.

Table 3 lists the recommended porous materials for removal of sulfide only, as well as removal of sulfide and  $\mathrm{CO}_2$  simultaneously. We can see that the optimum adsorbent is strongly dependent on the factors of the fluid systems and purification aims. Despite that zMOF is found to be the most suitable for removal of carbon and sulfide, the very high cost of indium metal may preclude its application for large-scale gas processing. It is expected this problem would be gradually solved in the future. In summary, by using computer simulations instead of expensive experiments, the complex screening process of potential materials can be easily and rapidly accomplished.





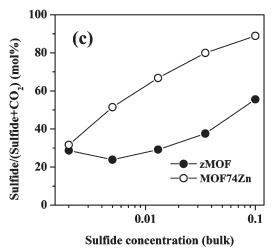


Figure 9. Effect of sulfide mole fraction in bulk phase on simultaneous removal of sulfide and CO<sub>2</sub> in the recommended porous materials at 4 MPa, where the closed and open symbols denote the CH<sub>4</sub>—CO<sub>2</sub>—H<sub>2</sub>S and N<sub>2</sub>—CO<sub>2</sub>—SO<sub>2</sub> systems, respectively.

# Effect of temperature on the selectivities and uptakes of screened adsorbents

Figure 6 shows the effect of temperature on the desulfurization of the CH<sub>4</sub>—CO<sub>2</sub>—H<sub>2</sub>S and N<sub>2</sub>—CO<sub>2</sub>—SO<sub>2</sub> systems

by the recommended adsorbents. For consistence with previous discussion, we used the simulated adsorption data at 4 M Pa for analysis. It is well known that increasing the temperature will usually reduce the selectivity. To our surprise, with the increase of temperature, a rising of selectivity occurs in both zeolites after a prior decrease (see Figure 6a). Figure 6b shows that the sulfide uptakes fall down slowly with the temperature. Hence, this rising can only be explained by the uptakes of other components like CO<sub>2</sub> decreasing sharper than sulfide. In contrast to zeolites, the adsorptions in MOFs are more noticeably influenced by the temperature. For instance, in the N2-CO2-SO2 system, the selectivity and uptake of MIL-47(V) give a drop of 92% and 95%, respectively, whereas for Na-13X it declines only 35% and 52% in the whole temperature range. From the standpoint of adsorbent regeneration, zeolites are clearly inferior to MOFs, because desorbing sulfide at a higher temperature will spend a more energy consuming. Especially, only given a slight increase of temperature (from 303 K increasing to 333 K), the H<sub>2</sub>S molecules are almost totally desorbed from the zMOF adsorbent. In this regard, zMOF is preeminent over other adsorbents and temperature swing adsorption is preferred for the removal of trace H<sub>2</sub>S impurities in zMOF. Figure 7a and b show that increasing temperature leads to a quick decrease of the selectivity and uptake of SO<sub>2</sub> and CO<sub>2</sub> in MOF-74-Zn, in contrast to a moderate decline in zMOF for simultaneous removal of H<sub>2</sub>S and CO<sub>2</sub>. This phenomenon can also be interpreted by the corresponding variation trends of sulfide percentage in Figure 7c.

# Effect of sulfide concentration on the selectivities and uptakes of recommended adsorbents

In general, the amount of sulfur (like H<sub>2</sub>S) in raw natural gas varies widely from parts per million levels up to 5%. Hence, it is necessary to explore the effect of the sulfide concentration on the separation performance of recommended adsorbents. Figures 8 and 9 show the dependence of the selectivity and uptake on sulfide concentration of bulk phase for removal of sulfide and simultaneous removal of sulfide and CO<sub>2</sub>, respectively. In both cases, the content of CH<sub>4</sub> or N<sub>2</sub> is fixed and we only increase the concentration of sulfide. We can see from Figure 8a when the bulk concentration of sulfide increases from 0.002 to 0.1, the selectivities of sulfide in both zeolites go down drastically and only give 1/70-1/80 of the original value. However, the uptakes of sulfide are nearly unchanged within the sulfide concentration range studied (see Figure 8b). According to Eq. 2, the change of sulfide bulk concentration will cut the selectivity to 1/50 of the original value. This implies that another contribution to this decrease arises from the increase of the total uptake of CH<sub>4</sub> and CO<sub>2</sub>. As shown in Figure 8c, the selectivity of MOFs for sulfide also descends with the increase of sulfide concentration, but with a relatively slow rate, compared to zeolites. Fortunately, the sulfur storage capacity of MOFs would double at a high sulfide concentration, despite sacrificing selectivity. All these observations indicate that MOFs offer an obvious advantage over zeolites for the gas purification containing high levels of sulfide contaminant.

Figure 9a shows that for simultaneous desulfurization and decarburization, there is a significant difference between the selectivities of MOF-74-Zn and zMOF. Apparently, the selectivity of MOF-74-Zn suddenly ascends with the bulk sulfide content, whereas it is almost unaltered for zMOF. Because the gas composition of  $CH_4$  or  $N_2$  in each system is fixed, the

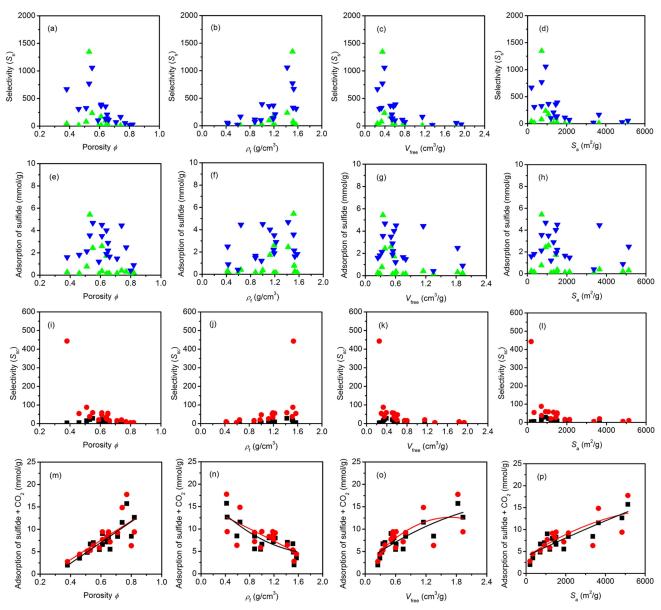


Figure 10. Adsorption selectivity and uptake versus porosity Φ, framework density ρ<sub>f</sub>, free pore volume V<sub>free</sub>, and accessible surface area S<sub>a</sub> at 4 MPa and 303 K, where the pyramid symbol denotes removal of sulfide for CH<sub>4</sub>—CO<sub>2</sub>—H<sub>2</sub>S, the inverted pyramid symbol denotes removal of sulfide for N<sub>2</sub>—CO<sub>2</sub>—SO<sub>2</sub>, the square symbol denotes removal of sulfide and CO<sub>2</sub> for CH<sub>4</sub>—CO<sub>2</sub>—H<sub>2</sub>S, and the circle symbol denotes removal of sulfide and CO<sub>2</sub> for N<sub>2</sub>—CO<sub>2</sub>—SO<sub>2</sub>. Lines are the guide to the eyes.

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change of bulk sulfide content would not affect the molar ratio of the gas components in Eq. 3. With the increase of bulk sulfide concentration, the total uptake of sulfide and  $CO_2$  in MOF-74-Zn increases monotonically (see Figure 9b). Furthermore, the percentage of sulfide in the total uptake increases pronouncedly. On the contrary, the total uptake of sulfide and  $CO_2$  in zMOF exhibits a decrease trend and then increases with the increase of bulk sulfide concentration (see Figure 9b). The similar behavior also appears in the curve of the percentage of sulfide in the total uptake of zMOF (see Figure 9c).

# Effect of material structure on the selectivities and uptakes of recommended adsorbents

To explore the effect of material structure on the separation ability of various adsorbents, the selectivities and uptakes at 4 MPa are plotted in Figure 10 as a function of the porosity  $\Phi$ , framework density  $\rho_{\rm f}$ , free pore volume  $V_{\rm free}$ , and accessible surface area  $S_{\rm a}$ . We can see that the optimum porosities  $\Phi$  for desulfurization center on about 0.5–0.6, where both the selectivity and uptake are the highest. Furthermore, a large framework density  $\rho_{\rm f}$  (~1.5 g cm<sup>-3</sup>), and a small free pore volume  $V_{\rm free}$  (~0.3 cm<sup>3</sup> g<sup>-1</sup>) and accessible surface area  $S_{\rm a}$  (~800 m<sup>2</sup> g<sup>-1</sup>) benefit to the removal of trace sulfide. For desulfurization and decarburization simultaneously, the optimum porosities  $\Phi$  is also found at 0.5–0.6 for their selectivities. However, the adsorption capacities of sulfide and  $CO_2$  are favored at high porosities. The effects of framework density  $\rho_{\rm f}$ , free pore volume  $V_{\rm free}$ , and accessible surface area  $S_{\rm a}$  on the selectivities of desulfurization/decarburization are similar to the case of desulfurization only.

Moreover, the uptakes of sulfide and CO<sub>2</sub> monotonically increase with the porosities  $\Phi$ , free pore volume  $V_{\text{free}}$ , and accessible surface area Sa, but decrease with the increase of framework density  $\rho_f$ , which is consistent with the pure CO<sub>2</sub> storage in MOFs by Babarao and Jiang. 38 Clearly, the impact of material structure on separation performance is dependent on the different aims at the applications of desulfurization only and simultaneous desulfurization/decarburization.

### **Conclusions**

We have performed a systematic molecular screening for porous carbons, zeolites, and MOFs to remove the sulfide and CO2 from the ternary mixtures. It is found that for desulfurization only, zeolites are superior to carbons and MOFs, while for simultaneous desulfurization and decarburization, MOFs are better than zeolites and carbons. For both applications, the MOF adsorbents are easier to regeneration than zeolites, because the adsorbed gases can be released quickly by increasing temperature. In addition, the selectivities of MOFs decline slower with the increase of sulfide concentration in bulk phase, compared to zeolites. On the contrary, the uptakes of MOFs increase more evidently than zeolites. It demonstrates that the MOFs are more suitable for the desulfurization of gas containing high concentration contaminant. The effects of material structure on the selectivities and uptakes of the recommended adsorbents have also been discussed. In summary, this work proposed a computational strategy to screen the known materials for gas separation in ternary mixtures. More importantly, by using this strategy, unknown materials can also be rapidly screened without expensive experiments. It is expected that the information obtained would provide a deep insight into materials and process design, development, and operating optimization in subsequent applications.

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